



**Dr. B. C. Roy Engineering College, Durgapur**  
**Basic Science and Humanities Department**  
**1<sup>st</sup> Semester**

**Paper: Physics I**      **CODE: BS-PH 101**      **AY: 2022-23**  
**Continuous Assessment-2**      **FM: 25**      **Date: 16-11-2022**

<b>Q. No.</b>	<b>Question</b>	<b>Marks</b>	<b>COs</b>	<b>BL</b>
<b>1.</b>	<b>Write a Report on applications of Gradient, Divergence and Curl in Engineering.</b>	<b>12</b>	<b>CO1</b>	<b>P</b>
<b>2.</b>	<b>Write the assumptions of Planck's radiation law hence derive the Planck's radiation law.</b>	<b>13</b>	<b>CO4</b>	<b>R, A</b>

- i) a) Plane
- ii) a) Angle of Scattering
- iv) c)  $\frac{h}{p}$
- v) c)  $180^\circ$
- vi) a)  $\hat{n} = \frac{\vec{A}}{|\vec{A}|}$
- ii) b) Never perfectly dark.

2) We know that,

$$\lambda' - \lambda = \frac{h}{m_0 c} (1 - \cos \phi)$$

$\Rightarrow \lambda' = \lambda + \frac{h}{m_0 c} (1 - \cos \phi)$

If we want the maximum wave length of the scattered ray then,

~~$\phi = 180^\circ$~~  should be  $180^\circ$

$$\Rightarrow \lambda' = 10^{-11} + \frac{6.626 \times 10^{-34}}{9.11 \times 10^{-31} \times 3 \times 10^8} (1 - (-1))$$

$$\Rightarrow \lambda' = 1.48 \times 10^{-11} \text{ m}$$

- $\lambda$  = Incident Wavelength =  $10^{-11} \text{ m}$
- $\lambda'$  = Scattered <sup>rays</sup> wavelength = ?
- $h$  = Planck's constant =  $6.626 \times 10^{-34} \text{ J-sec}$
- $m_0$  = mass of the electron =  $9.11 \times 10^{-31} \text{ kg}$
- $c$  = Speed of Light =  $3 \times 10^8 \text{ m/s}$
- $\phi$  = Angle of scattering =  $180^\circ$

$\therefore$  The maximum wavelength present in the scattered rays are  $1.48 \times 10^{-11} \text{ m}$

$\therefore$  The kinetic energy,  $E = (h\nu - h\nu')$  /  $\nu = \text{frequency of that ray}$

$$\begin{aligned} \Rightarrow E &= h \left( \frac{c}{\lambda} - \frac{c}{\lambda'} \right) = hc \left( \frac{1}{\lambda} - \frac{1}{\lambda'} \right) \\ &= 6.626 \times 10^{-34} \times 3 \times 10^8 \times \left( \frac{1}{10^{-11}} - \frac{1}{1.48 \times 10^{-11}} \right) \\ &= 6.45 \times 10^{-15} \end{aligned}$$

$\therefore$  The maximum kinetic energy of the recoil electron is  $6.45 \times 10^{-15} \text{ Jule} = 40312.5 \text{ eV} = 40.3125 \text{ keV}$

3)  
a)

We know that

Phase velocity,  $v_p = \frac{\omega}{k}$   
Group velocity,  $v_g = \frac{d\omega}{dk}$

$\omega = \text{angular frequency}$   
 $k = \frac{2\pi}{\lambda} = \text{proportional constant.}$   
 $\lambda = \text{wavelength.}$

$$\therefore v_p = \frac{\omega}{k}$$

$$\Rightarrow \omega = v_p k$$

Differ. w.r.t  $k$ . We get,

$$\Rightarrow \frac{d\omega}{dk} = v_p + k \cdot \frac{dv_p}{dk}$$

$$\Rightarrow \frac{d\omega}{dk} = v_p + k \cdot \frac{v_p}{d\lambda} \cdot \frac{d\lambda}{dk}$$

$$\Rightarrow \frac{d\omega}{dk} = v_p + \frac{2\pi}{\lambda} \cdot \frac{v_p}{d\lambda} \cdot \left( -\frac{\lambda^2}{2\pi} \right)$$

$$\Rightarrow \boxed{\frac{d\omega}{dk} = v_p - \lambda \cdot \frac{v_p}{d\lambda}}$$

$$\begin{aligned} k &= \frac{2\pi}{\lambda} \\ \Rightarrow dk &= -\frac{2\pi}{\lambda^2} d\lambda \\ \Rightarrow \frac{d\lambda}{dk} &= -\frac{\lambda^2}{2\pi} \end{aligned}$$

b) Heisenberg says that, Product of the uncertain position ( $\Delta x$ ) and momentum ( $\Delta p$ ) of a particle in simultaneous measurement is equal to or greater than to  $\frac{h}{4\pi}$

Equation

$$\Delta x \cdot \Delta p \geq \frac{h}{4\pi}$$

Physical Significance :-

We can not find the both of position and momentum of a particle such as, electron, photon ~~etc~~ with perfect accuracy. When we ~~know~~ nail the position of the particle, the less we ~~get~~ know about the speed of the particle and vice versa.

### Interference

- i) ~~Interference occurs.~~
- i) The fringes are perfectly ~~dark~~ dark
- ii) The intensity of the maxima is bright
- iii) The fringes are of same width
- iv) ~~The bright~~ between It occurs ~~at~~ two coherent wavelength

### Diffraction

- i) The fringes are not perfectly dark.
- ii) The intensity of the maxima is not bright
- iii) The fringes ~~are~~ ~~not~~ width are varies.
- iv) It occurs between a large number of different coherent wavelength.

4/b)

We know that,

$$\lambda = a \sin \theta$$

When,  $\theta$  is very small

$$\sin \theta \approx \theta$$

$$\therefore \lambda = a \theta$$

$$\Rightarrow \theta = \frac{\lambda}{a} = \frac{6000 \times 10^{-10}}{0.1 \times 10^{-3}}$$

$$\Rightarrow \theta = 6 \times 10^{-3}$$

$$\Rightarrow 2\theta = 12 \times 10^{-3} \quad [\text{As } \theta \text{ is one side angular width of central maxima}]$$

$\therefore$  The angular width of the central maxima is  $12 \times 10^{-3}$  rad.

5/08)

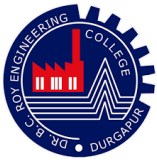
$$\vec{F} = \nabla (x^3 + y^3 + z^3 - 3xyz)$$

$$= \left( \frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) (x^3 + y^3 + z^3 - 3xyz)$$

$$= (3x^2 - 3yz) \hat{i} + (3y^2 - 3xz) \hat{j} + (3z^2 - 3xy) \hat{k}$$

$$\begin{aligned} \therefore \nabla \cdot \vec{F} &= \left( \frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) \cdot \left\{ (3x^2 - 3yz) \hat{i} + (3y^2 - 3xz) \hat{j} + (3z^2 - 3xy) \hat{k} \right\} \\ &= 6x + 6y + 6z \\ &= 6(x + y + z) \end{aligned}$$

$$\begin{aligned} \nabla \times \vec{F} &= \left( \frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) \times \left\{ (3x^2 - 3yz) \hat{i} + (3y^2 - 3xz) \hat{j} + (3z^2 - 3xy) \hat{k} \right\} \\ &= 0 \quad [\text{As, } \hat{i} \times \hat{i} = 0, \hat{j} \times \hat{j} = 0, \hat{k} \times \hat{k} = 0] \end{aligned}$$



**Full Marks: 25**

**Session- 2022-23**

**Time: 50 mins.**

**Continuous Assessment – 3**

Q. No.	Question	Marks	COs	BL
<b>GROUP –A (Multiple Choice Type Questions)</b>				
<b>Choose the correct answer for any five of the following:</b>				
1.	In Fraunhofer diffraction, the incident wave front is	1	CO2	<b>R</b>
(i)	(a) Plane (b) Cylindrical (c) Spherical (d) None of these			
(ii)	In Fraunhofer diffraction minima are	1	CO2	<b>R</b>
	(a) All perfectly dark (b) Never perfectly dark (c) Perfectly bright (d) None of these			
(iii)	The Compton Shift depends on	1	CO4	<b>U</b>
	(a) Angle of scattering (b) Material of the target (c) Wavelength of the incident X-ray (d) None of these			
(iv)	The de-Broglie wavelength of a particle with momentum p is	1	CO4	<b>R</b>
	(a) $\frac{h}{p^2}$ (b) $\frac{p^2}{h^2}$ (c) $\frac{h}{p}$ (d) $\frac{p}{h^2}$			
(v)	The Compton shift is maximum when the scattering angle is	1	CO4	<b>E</b>
	(a) $45^\circ$ (b) $90^\circ$ (c) $180^\circ$ (d) $60^\circ$			
(vi)	If $\hat{n}$ is the unit vector in the direction $\vec{A}$ then	1	CO1	<b>P</b>
	(a) $\hat{n} = \frac{\vec{A}}{ \vec{A} }$ (b) $\hat{n} = \vec{A}  \vec{A} $ (c) $\hat{n} = \frac{ \vec{A} }{\vec{A}}$ (d) None of these			
<b>GROUP – B (Short Answer Type Questions)</b>				
<b>Answer all the questions from the following</b>				
2.	X-rays of wavelength $10^{-11}$ m are scattered by loosely bound electrons. Find the maximum wavelength present in the scattered rays and maximum kinetic energy of the recoil electron.	3 + 2	CO4	<b>E</b>
3.	(a) Find the relation between Phase velocity and Group velocity.	2 + 3	CO4	<b>P</b>
	(b) Write the Heisenberg's uncertainty principle and explain its physical significance.			<b>R</b>
4.	(a) Differentiate Interference and Diffraction. (b) A light of $6000\text{\AA}$ falls normally on a straight slit of 0.1mm width. Calculate the total angular width of the central maxima.	3 + 2	CO2	<b>R</b> <b>E</b>
	<b>OR</b>			
	Define the terms and find the expressions in connection with damped vibration (a) Decay Constant (b) Logarithmic decrement	2 + 3	CO1	<b>A</b>
5	What is Brewster's law in polarization of light? Show that sum of angle of polarization and angle of refraction is $90^\circ$ .	1 + 4	CO2	<b>R</b> <b>E</b>
	<b>OR</b>			
	Find $\vec{\nabla} \cdot \vec{F}$ and $\vec{\nabla} \times \vec{F}$ where $\vec{F} = \vec{\nabla}(x^3 + y^3 + z^3 - 3xyz)$	1.5+ 1.5+2	CO1	<b>E</b>
	<b>OR</b>			
	Establish the differential equation of damped vibration and solve it.	2 + 3	CO1	<b>A</b>

