



**Intelligent Technologies: Concepts, Applications, and Future Directions** pp 281–312

## Development of Fuzzy-Based Methodologies for Decision-Making Problem

[Avijit De](#) , [Samarjit Kar](#) & [Sujit Das](#)

Chapter | [First Online: 22 May 2022](#)

**59** Accesses

Part of the [Studies in Computational Intelligence](#) book series (SCI, volume 1028)

### Abstract

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Decision-making is a crucial task of our life. In the real world, the decision parameters of most decision-making problems are imprecise and ambiguous in nature, which makes the problems uncertain. To solve uncertain problems, fuzzy sets (FSs) along with its various extensions perform a crucial part in decision-making paradigm. In this thesis, we have presented approaches to tackle with decision-making problems using FS extensions such as the interval type-2 fuzzy set (IT2FS), probabilistic interval-valued intuitionistic hesitant fuzzy set (P-IVIHFS) and interval-valued

intuitionistic linear Diophantine fuzzy set (IVILDFS). We have developed an interactive decision-making approach on fuzzy production inventory using granular differentiability. The centroid index, rank index, and correlation coefficient are used in the proposed IT2FS ranking technique. Extended TOPSIS and VIKOR methods are studied to solve multi-attribute group decision-making (MAGDM) problems in the framework of P-IVIHFS. We have introduced IVILDFS as an extension of the linear Diophantine fuzzy set (LDFS). Score functions, accuracy functions and aggregation operators are proposed in the framework of IVILDFS and implemented to tackle decision-making problems. Preservation technology is used in the fuzzy production model to control the deterioration rate of the product, and granular differentiability approach is used for defuzzification. The proposed techniques are illustrated using numerical examples and comparative studies.

Keywords

**Multi-criteria decision-making      IT2FS**

**Centroid point value      Correlation coefficient**

**Mellin transform      P-IVIHFS      TOPSIS method**

**VIKOR method      IVILDFS**

**Fuzzy optimal control (FOC)**

**Granular differentiability**

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75. De A, Das S, Kar (2021) Ranking of interval type 2 fuzzy numbers using correlation coefficient and Mellin transform. *OPSEARCH* 1–31

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## Author information

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Authors and Affiliations

**Department of Mathematics, Dr. B. C. Roy  
Engineering College, Durgapur, India**

Avijit De

**Department of Mathematics, National Institute of  
Technology Durgapur, Durgapur, India**

Samarjit Kar

**Department of Computer Science and  
Engineering, National Institute of Technology  
Warangal, Warangal, India**

Sujit Das

Corresponding author

Correspondence to [Avijit De.](#)

## Editor information

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### Cite this chapter

De, A., Kar, S., Das, S. (2022). Development of Fuzzy-Based Methodologies for Decision-Making Problem. In: Dash, S.R., Lenka, M.R., Li, K.C., Villatoro-Tello, E. (eds) Intelligent Technologies: Concepts, Applications, and Future Directions. Studies in Computational Intelligence, vol 1028. Springer, Singapore. [https://doi.org/10.1007/978-981-19-1021-0\\_12](https://doi.org/10.1007/978-981-19-1021-0_12)

[.RIS](#)  [.ENW](#)  [.BIB](#) 

### DOI

[https://doi.org/10.1007/978-981-19-1021-0\\_12](https://doi.org/10.1007/978-981-19-1021-0_12)

Published	Publisher Name	Print ISBN
22 May 2022	Springer, Singapore	978-981-19-1020- 3

Online ISBN	eBook Packages
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